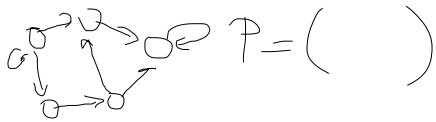


Markov



$X_1, X_2, X_3, X_4, X_5$

$S = \{0, 1, 2, 3, 4, 5, 6\}$

$31025201601231 \rightarrow P$

$P(X_1, X_2, \dots, X_n) = P(X_1=x_1)P(X_2|x_1)P(X_3|x_2)$

$= P(x_1) \prod_{i=1}^{n-1} P_{x_i x_{i+1}} = P(x_1) \prod_{i,j} P_{ij}^{n_{ij}}$

MLE  $L(p) = P(x_1) \prod_{i,j} P_{ij}^{n_{ij}}$

$\mathcal{L}(p) = \log L(p) = \log P(x_1) + \sum_{i,j} n_{ij} \log P_{ij}$

$\frac{\partial \mathcal{L}}{\partial P_{ij}} = 0$

$\mathcal{L}' = \mathcal{L} - \sum_i \lambda_i (\sum_j P_{ij} - 1)$

$\frac{\partial \mathcal{L}'}{\partial P_{ij}} = 0 = \frac{n_{ij}}{P_{ij}} - \lambda_i = 0$

$P_{ij} = \frac{n_{ij}}{\lambda_i} \quad \sum_j P_{ij} = 1 \Rightarrow$

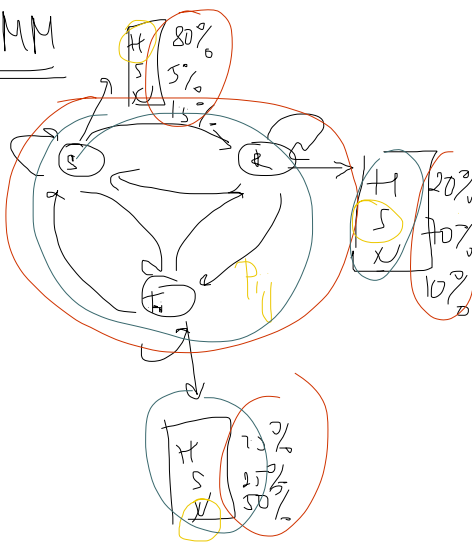
$\sum_j \frac{n_{ij}}{\lambda_i} = 1, \lambda_i = \frac{1}{\sum_j n_{ij}}$

$P_{ij} = \frac{n_{ij}}{\sum_j n_{ij}}$

$P_{11} = 0$   
 $P_{34} = \frac{1}{2}$   
 $P_{31} = \frac{1}{2}$

3 4 2 3 1 0 3 0 2 7 1 4 5 6 4 2 7

HMM



H H S X S S S H H X S H H H

$A = (a_{ij}) \left| \begin{matrix} \leftarrow \text{emission} \\ \leftarrow \text{transition} \end{matrix} \right.$

$B = (b_{ij}) \left| \begin{matrix} \leftarrow \text{emission} \\ \leftarrow \text{transition} \end{matrix} \right.$

$\pi \leftarrow H, y_i$

$\lambda = (A, B, \pi)$  HMM

$O = O_1 O_2 O_3 \dots$